

# Watermarking with Retrieval System

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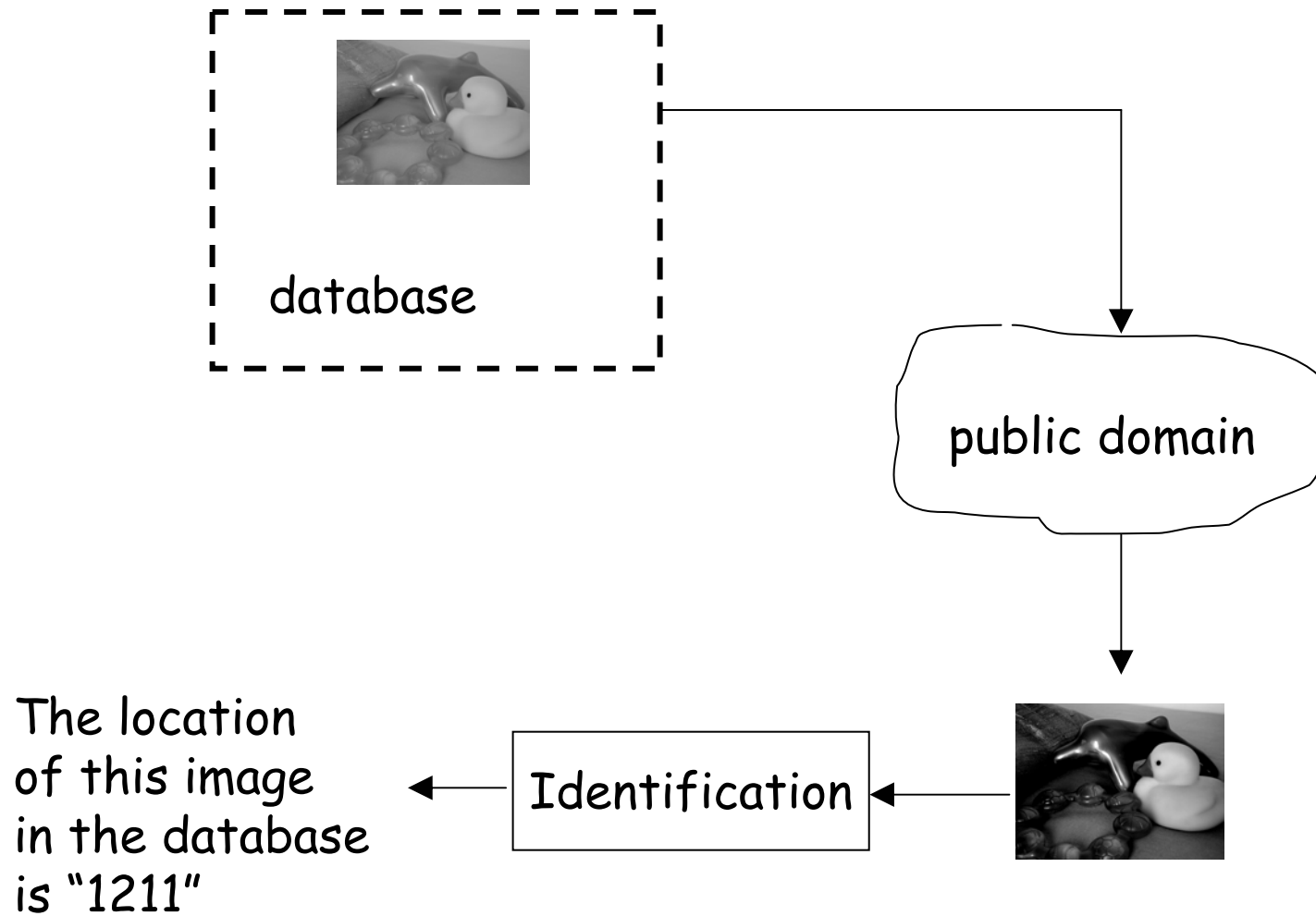
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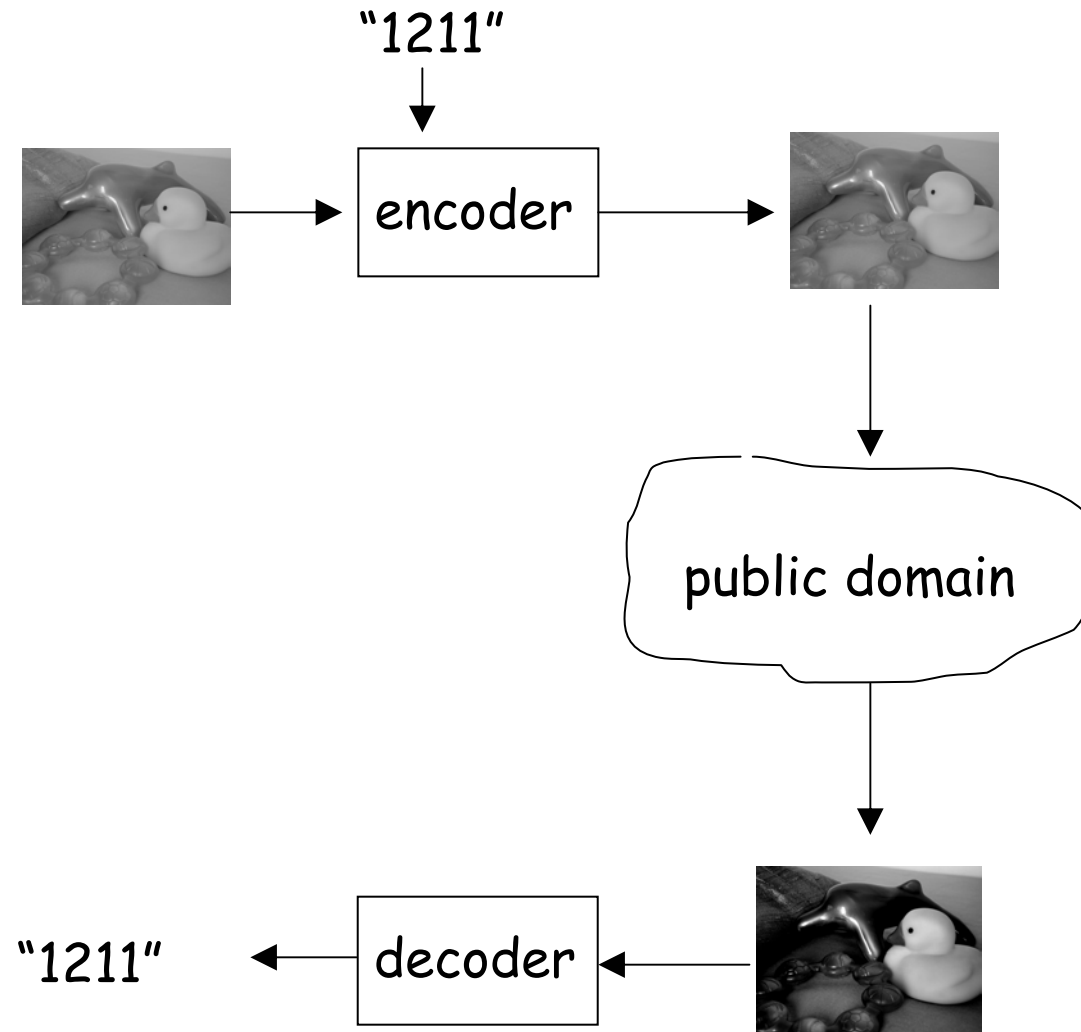
# Outlines of this talk:

- Describe the identification/tracking problem
- Can be addressed by 1) Watermarking, or  
2) Retrieval systems.
- Propose a tradeoff of 1) and 2).

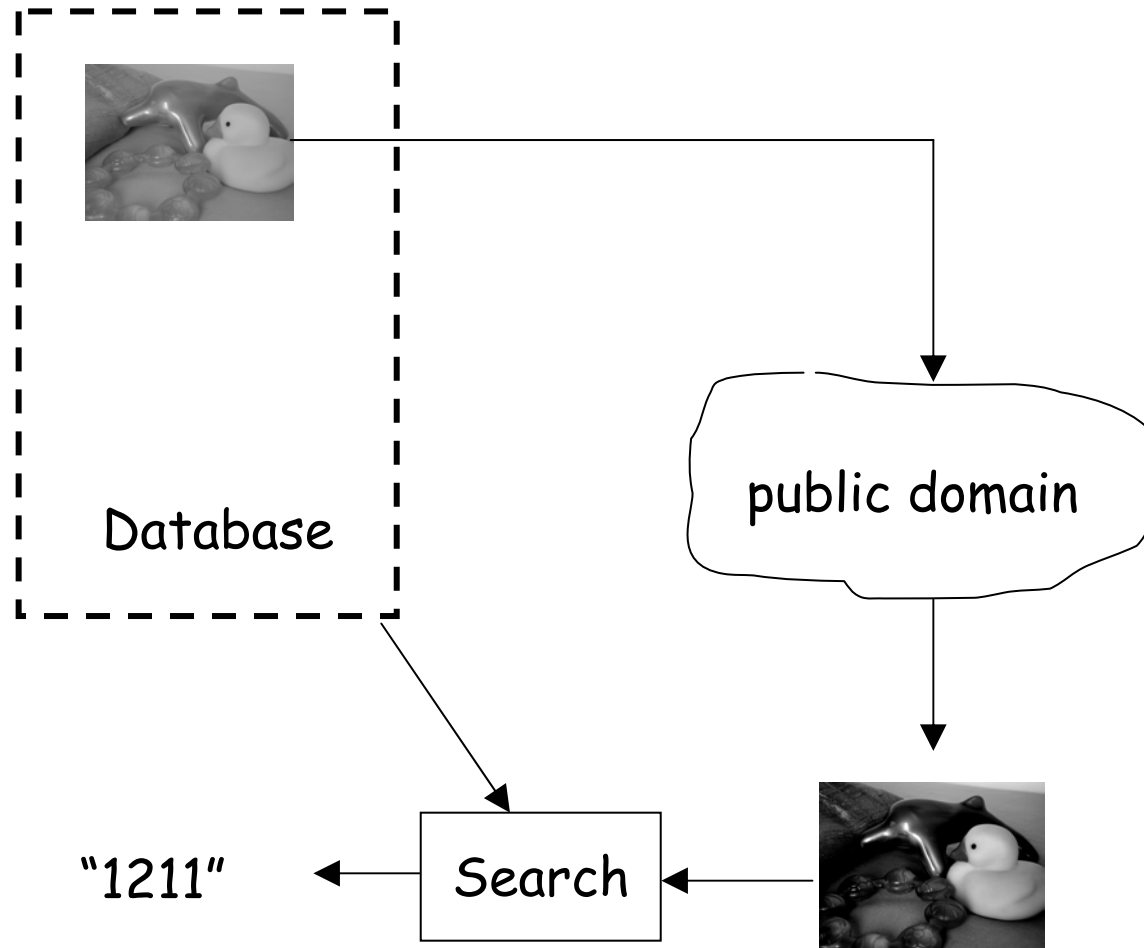
# Identification/tracking



# Identification/tracking by Watermarking



# Identification/tracking by Retrieval



# Research Goal:

- Retrieval systems: Slow searching (dimensionality curse), might causes ambiguity, no distortion.
- Watermarking: Fast decoding, resolve ambiguity, distortion.
- We propose to study tradeoff of these two extremes.

Image Space

Only watermarking...

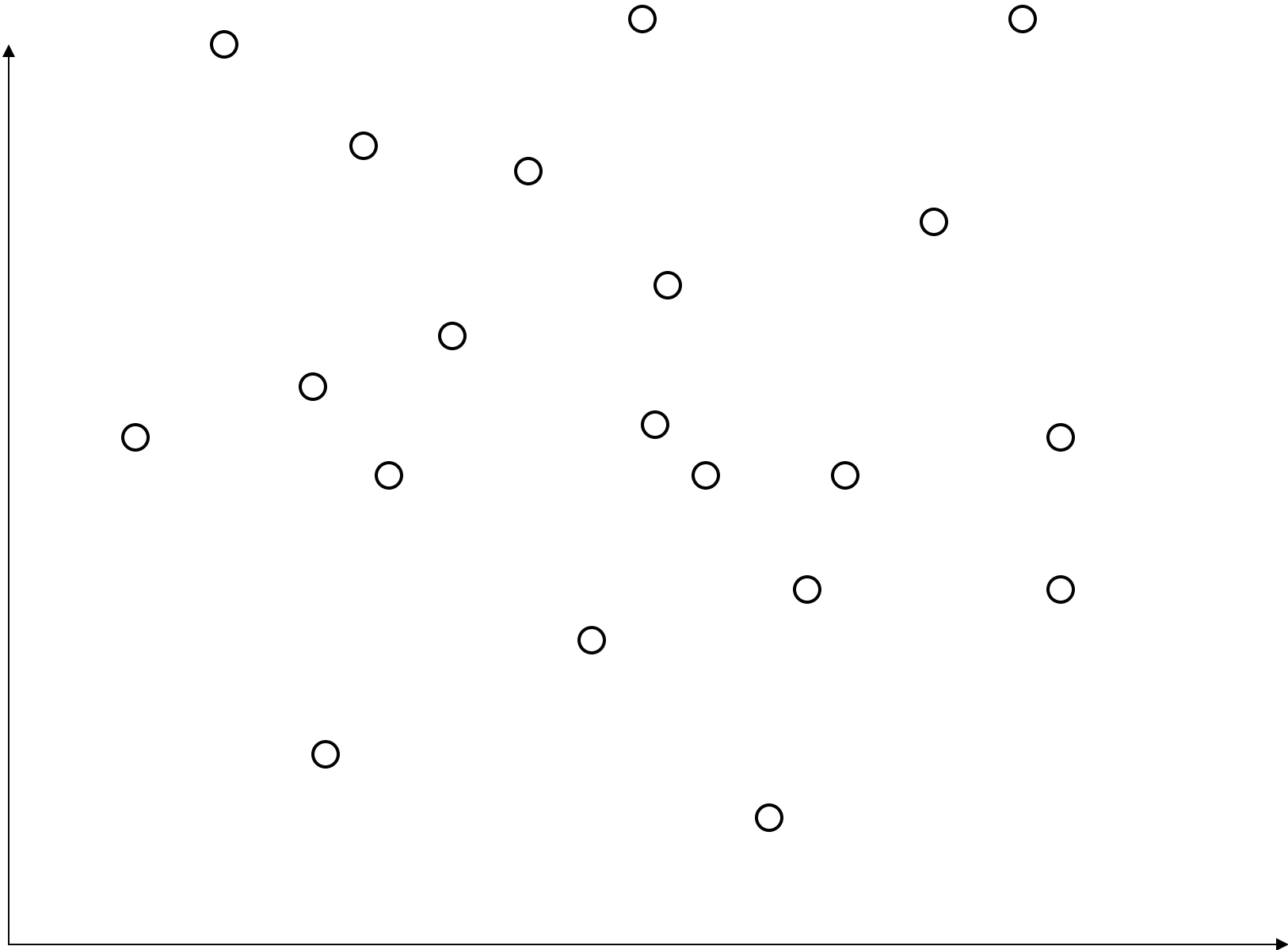


Image Space

Only watermarking...

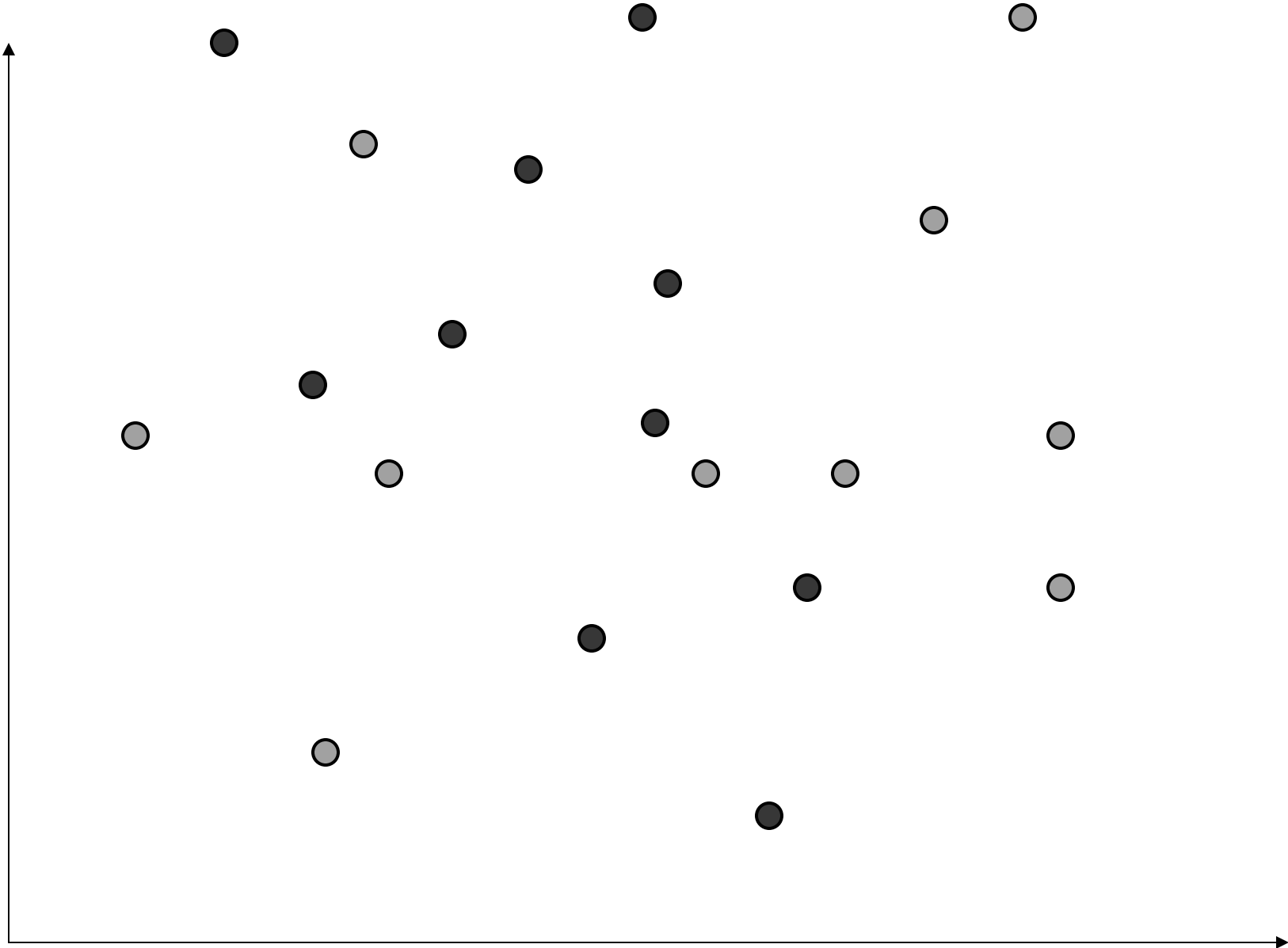




Image Space

Only watermarking...

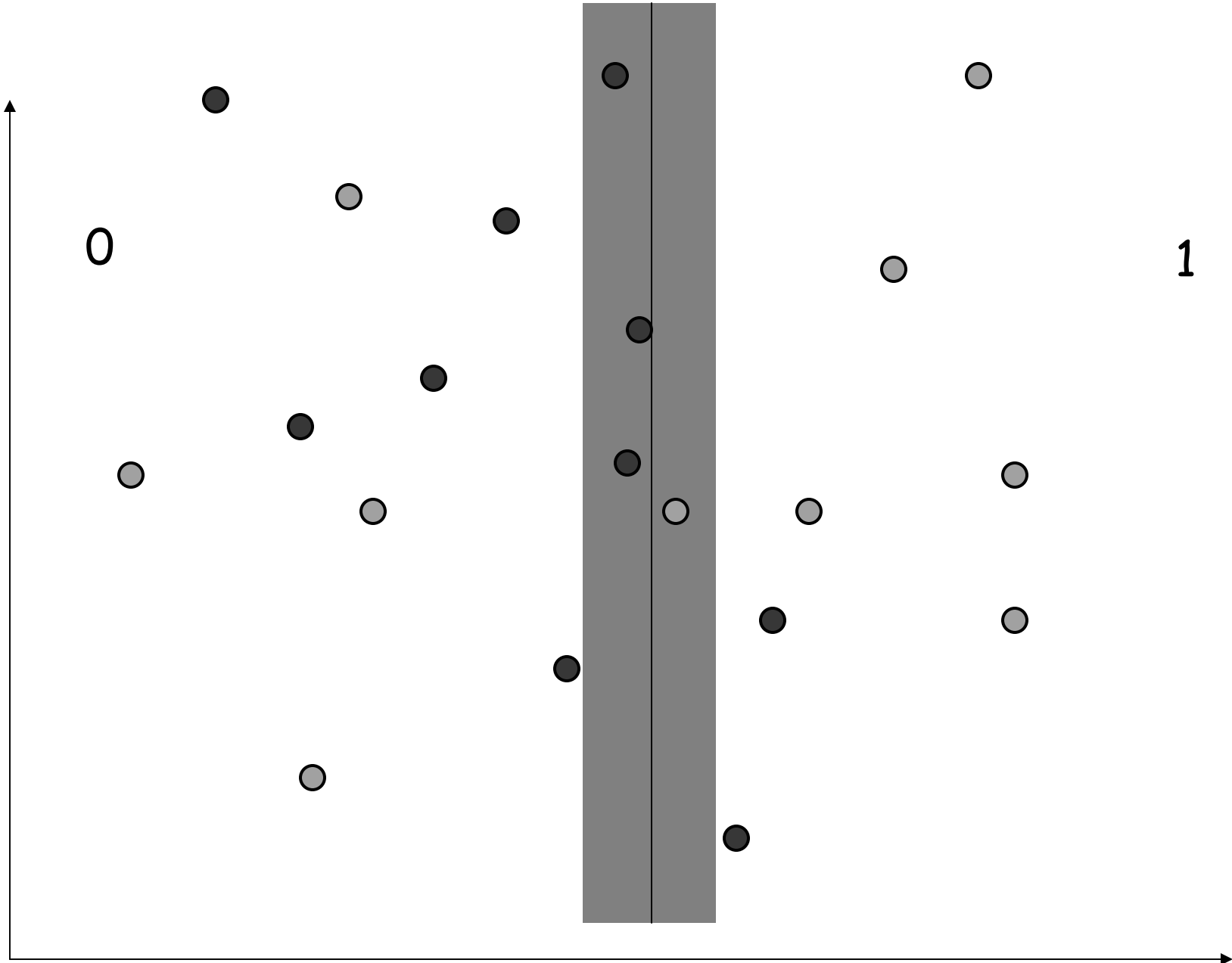


Image Space

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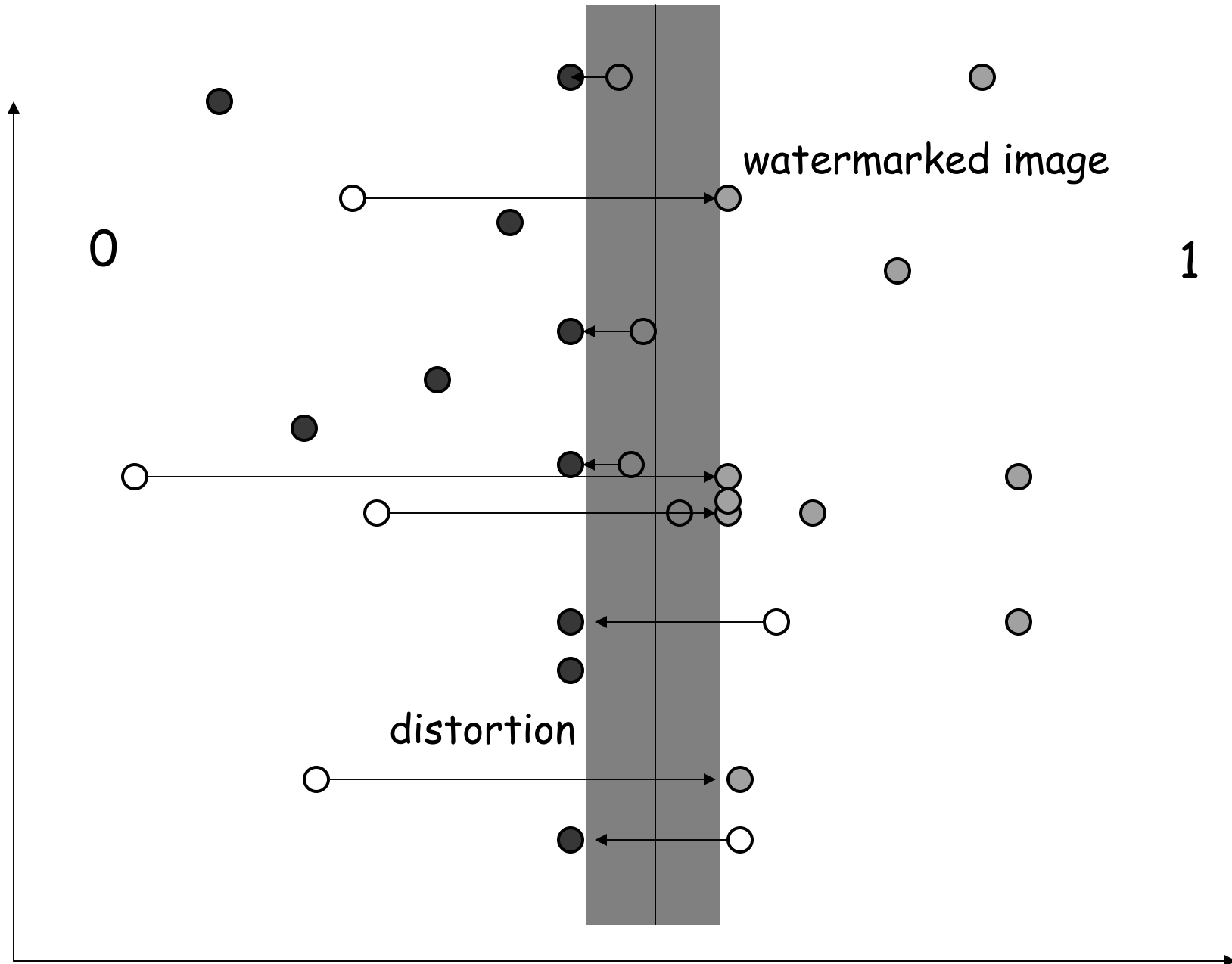


Image Space

Only by Retrieval...

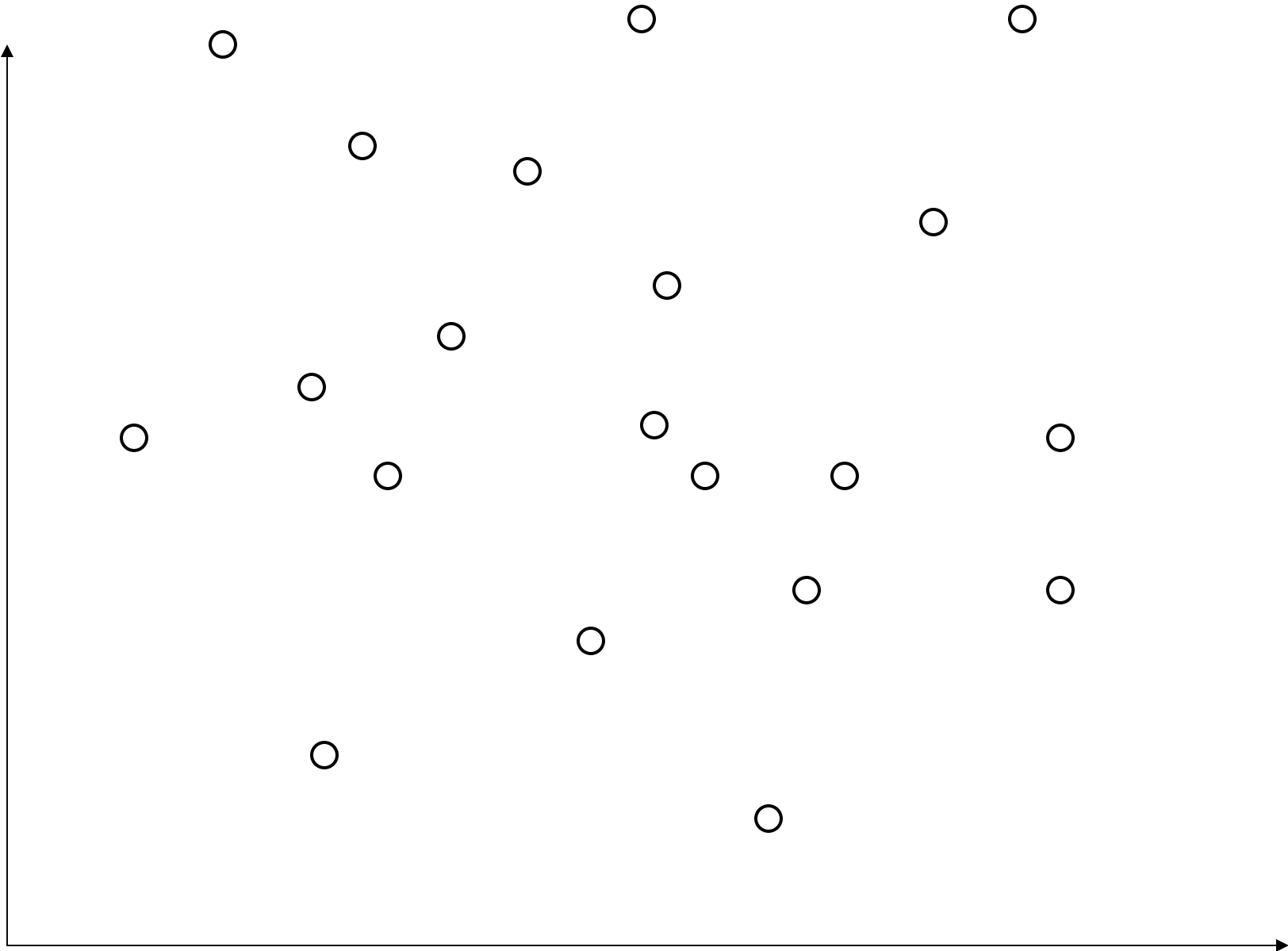


Image Space

Only by Retrieval...

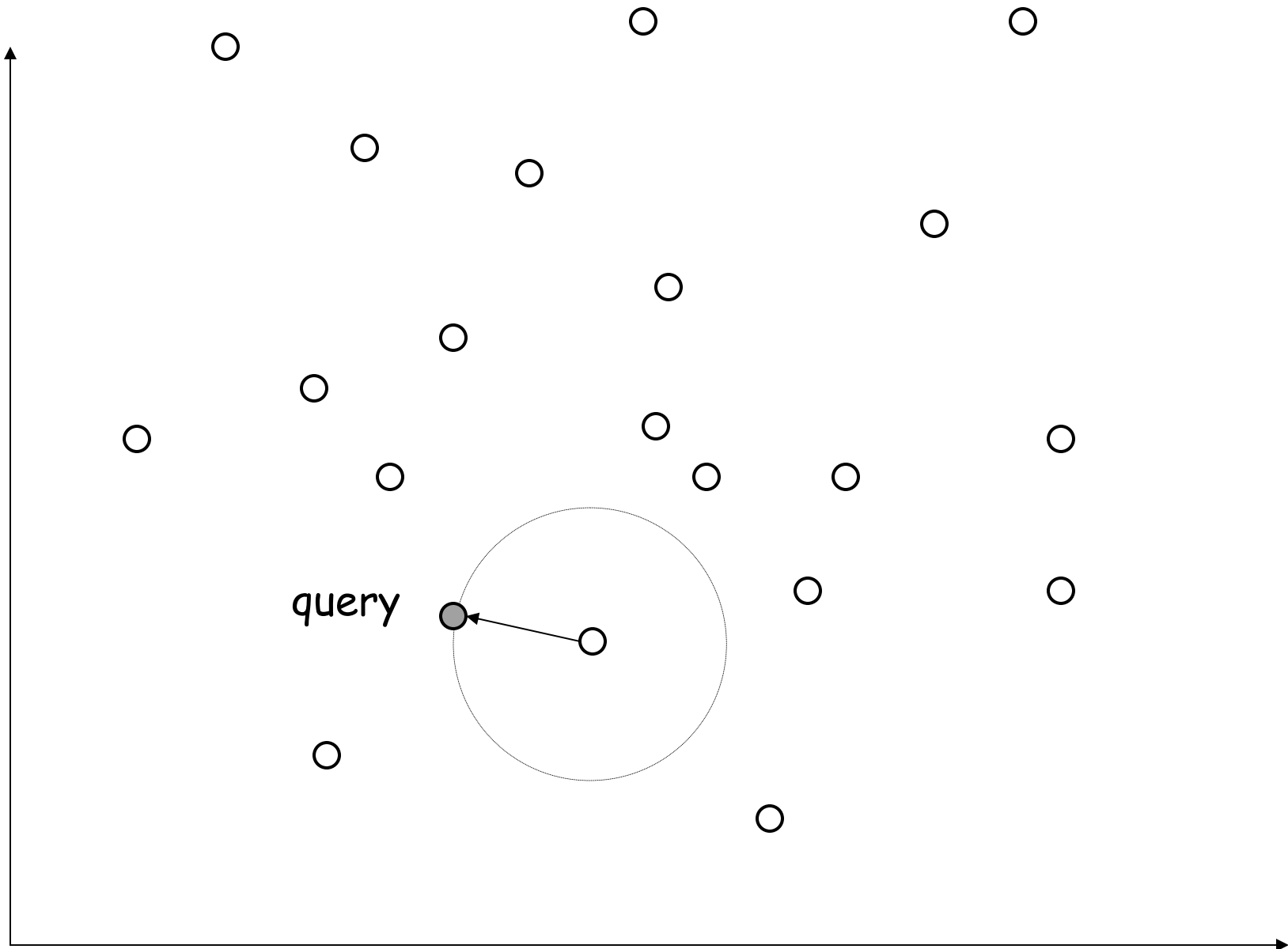


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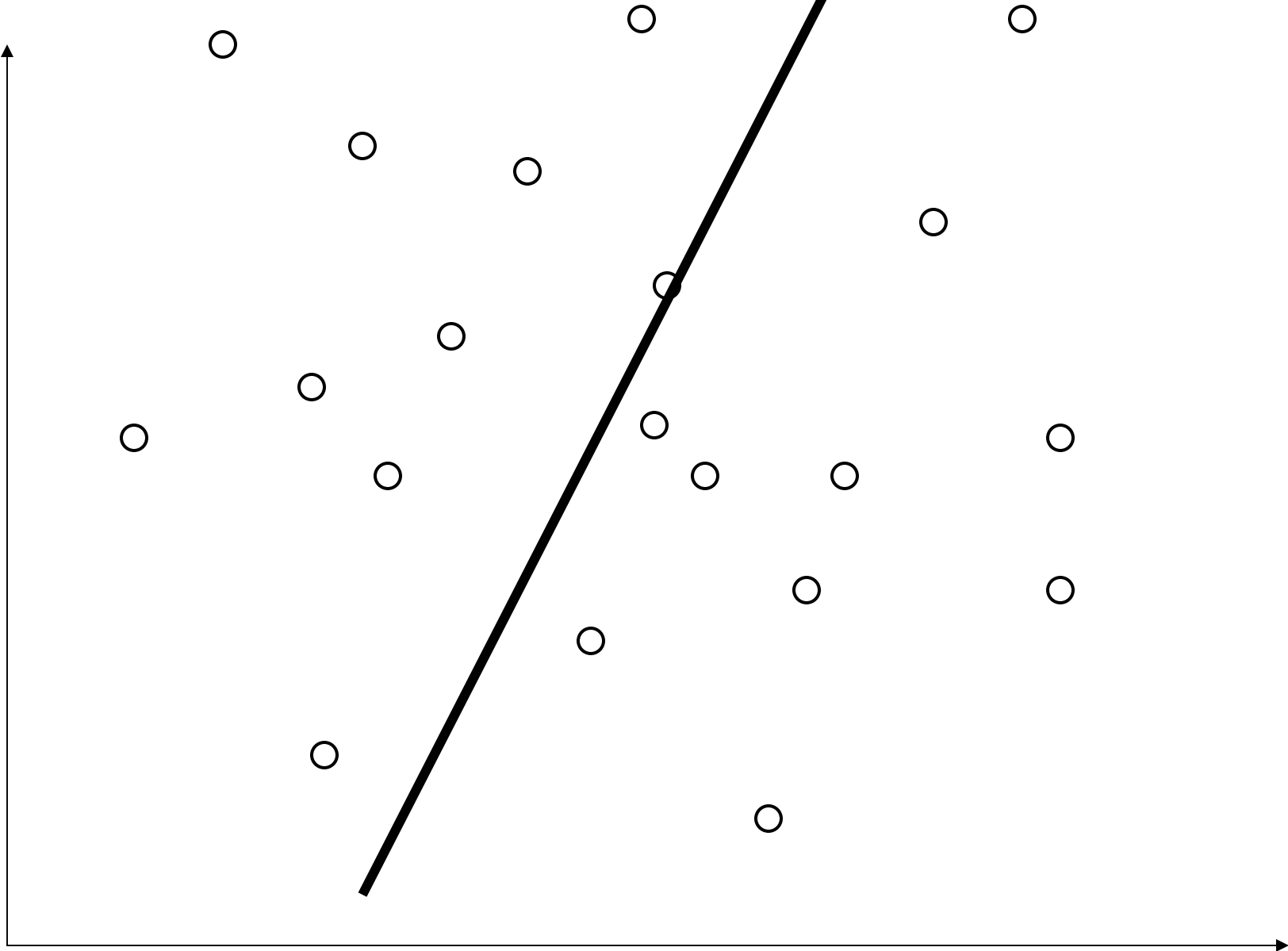


Image Space

Only by Retrieval...

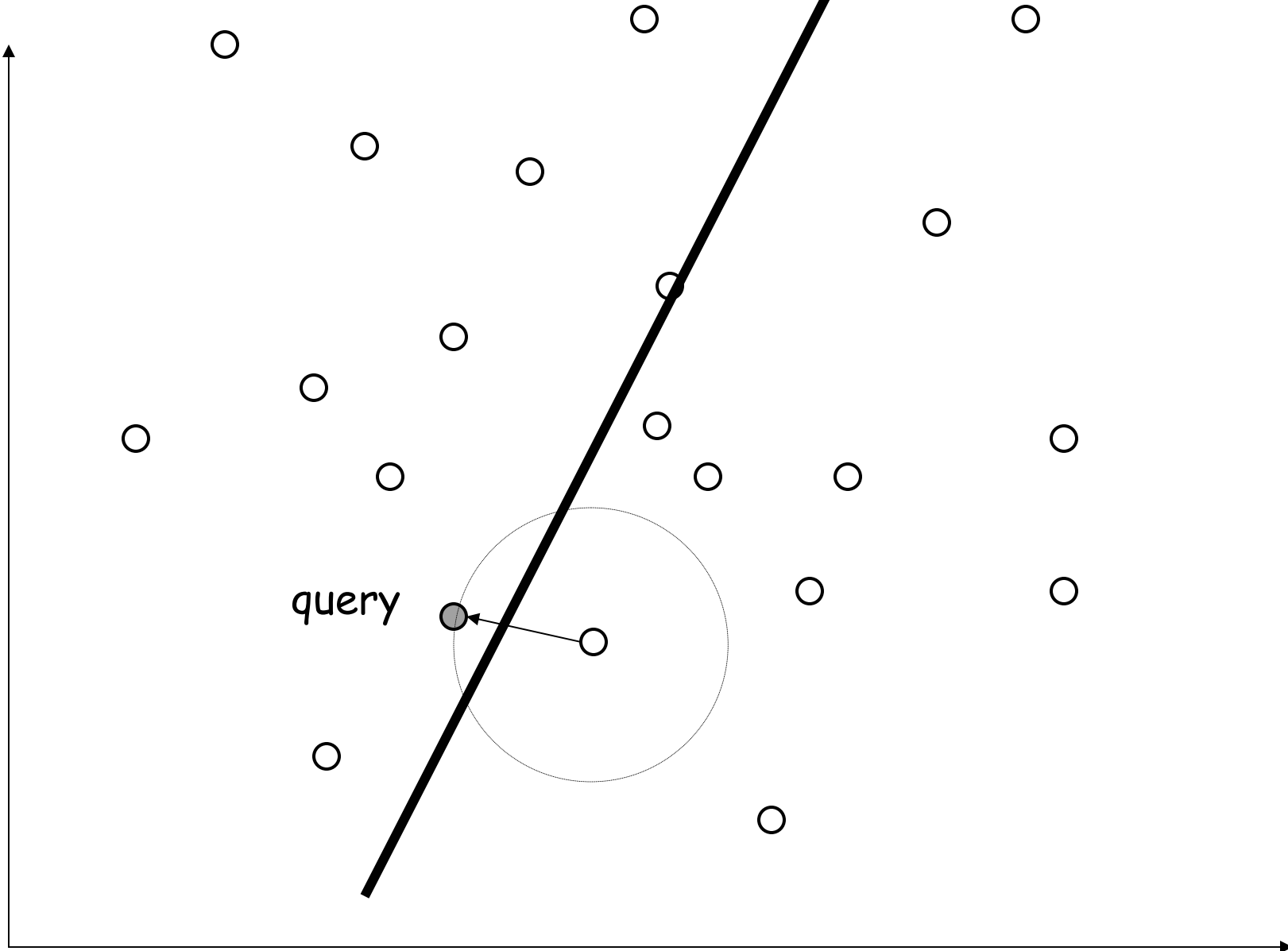


Image Space

Proposed method

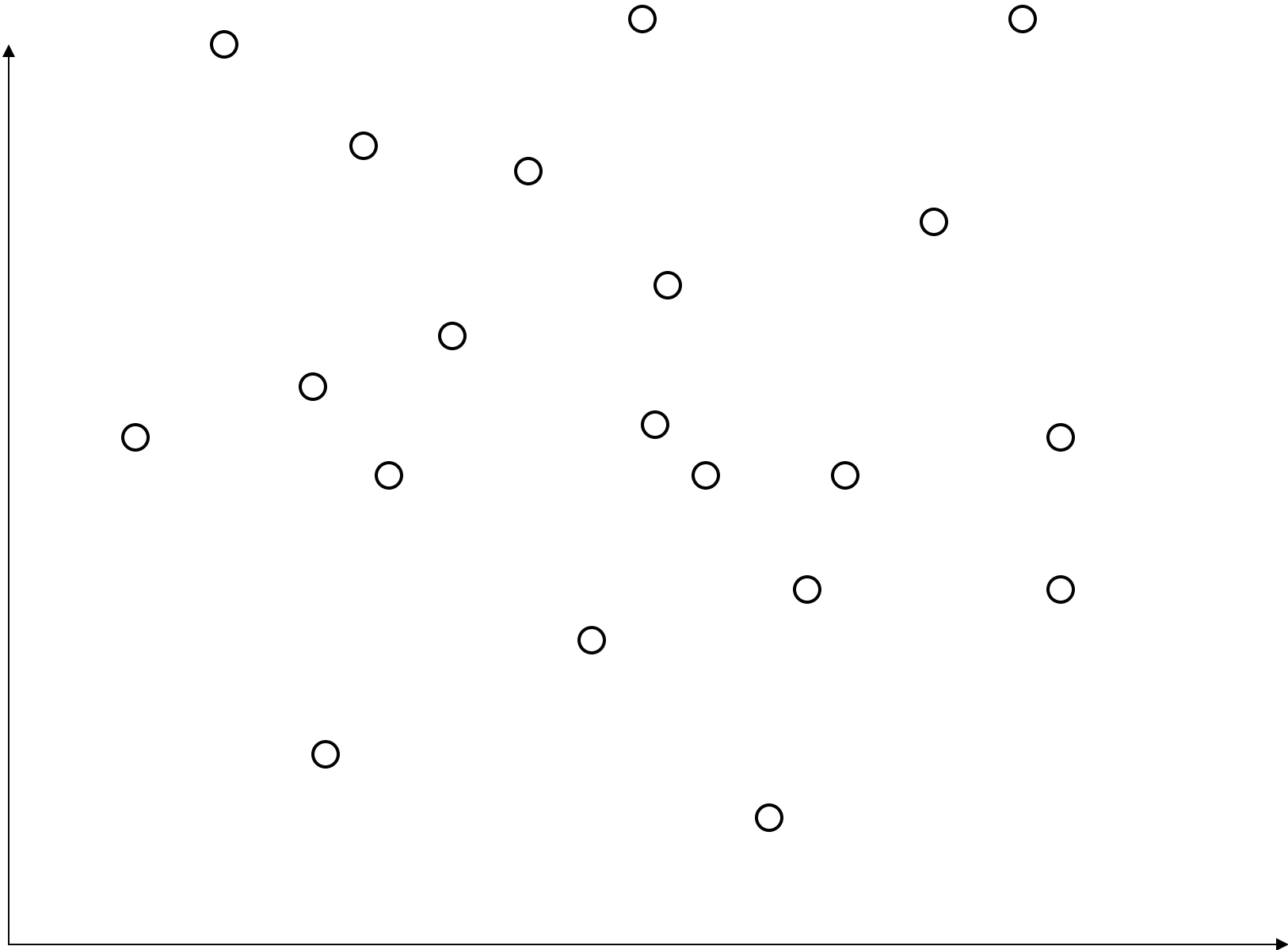


Image Space

Proposed method

Buffer Zone

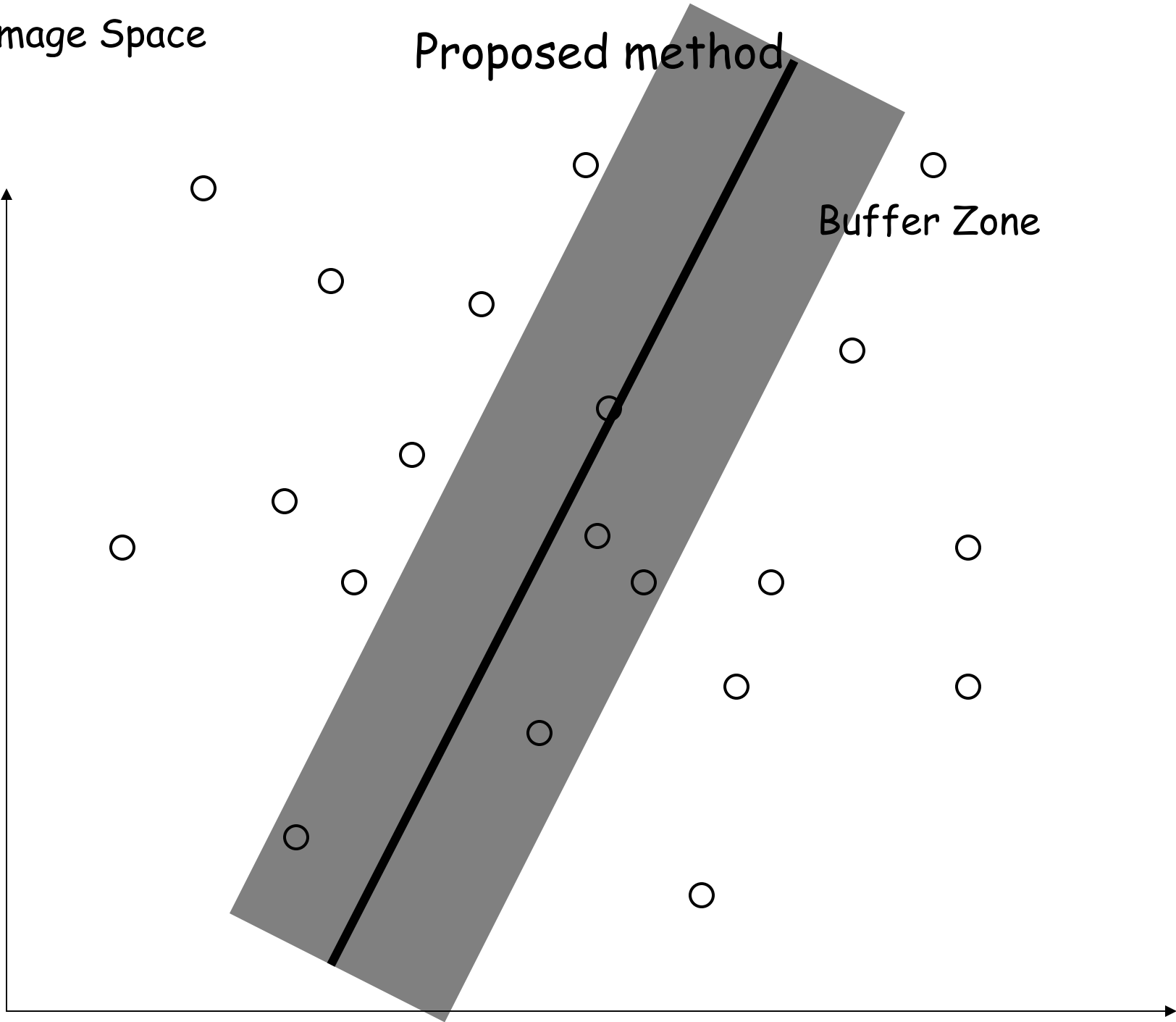


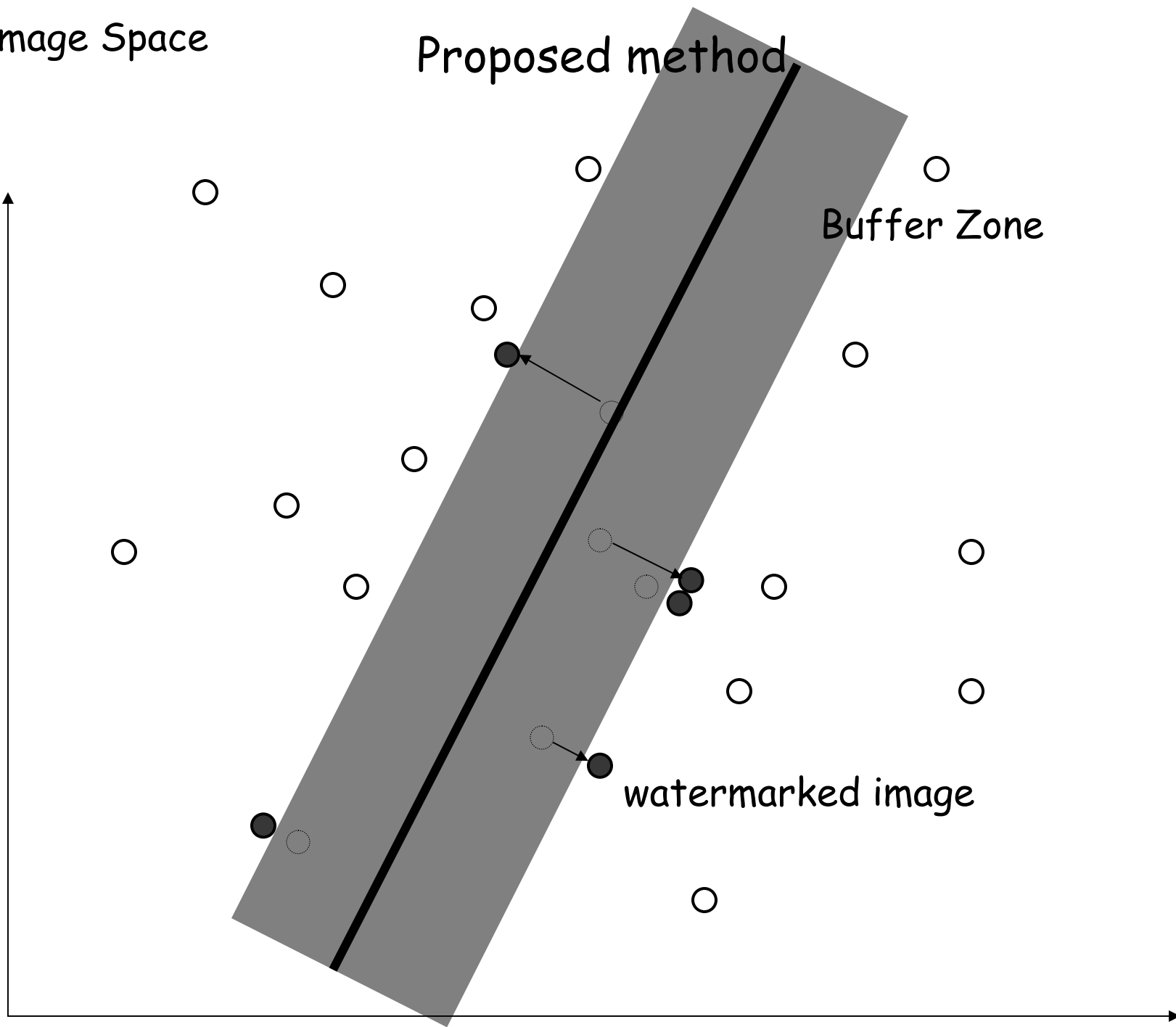


Image Space

Proposed method

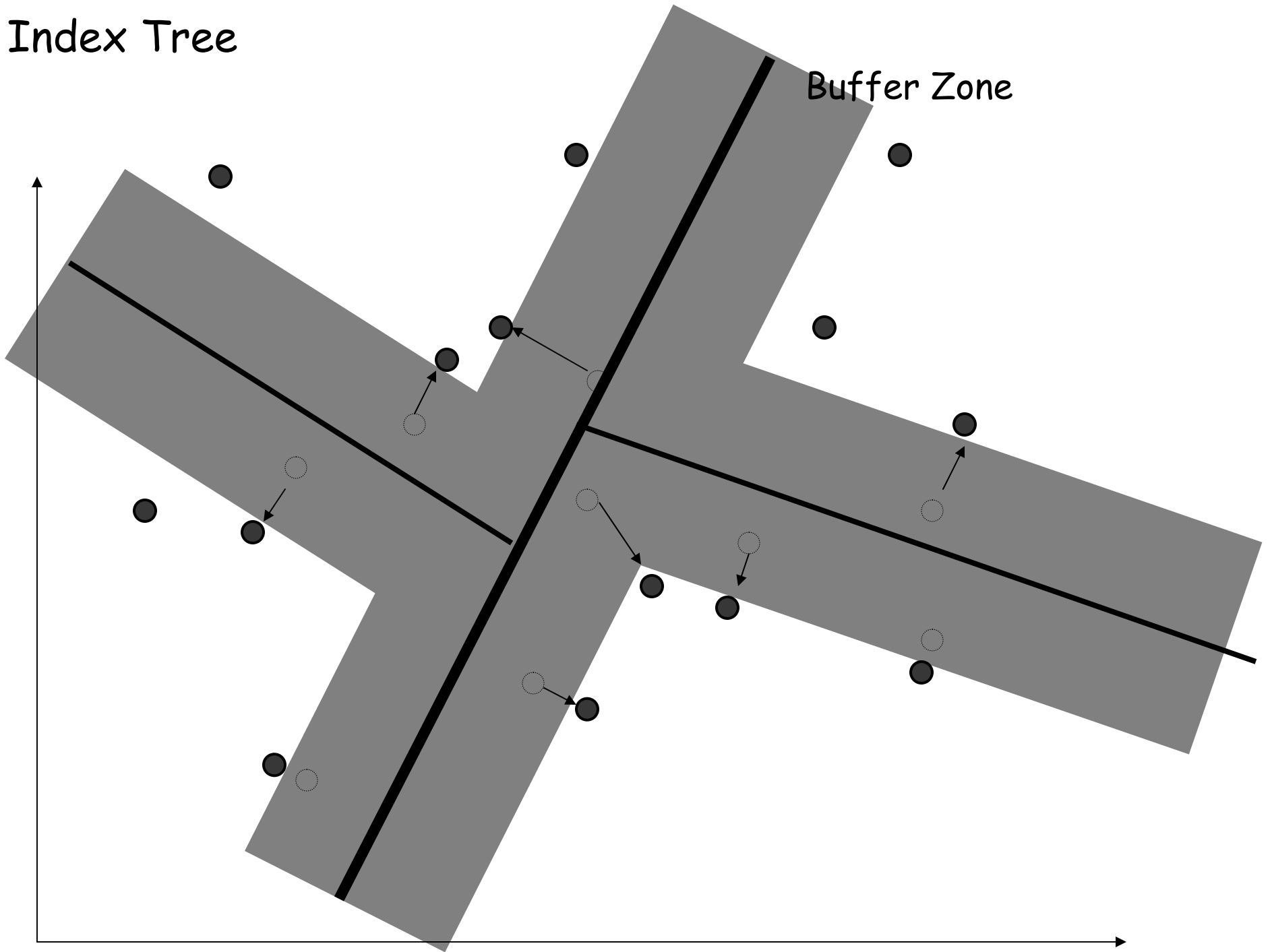
Buffer Zone

watermarked image

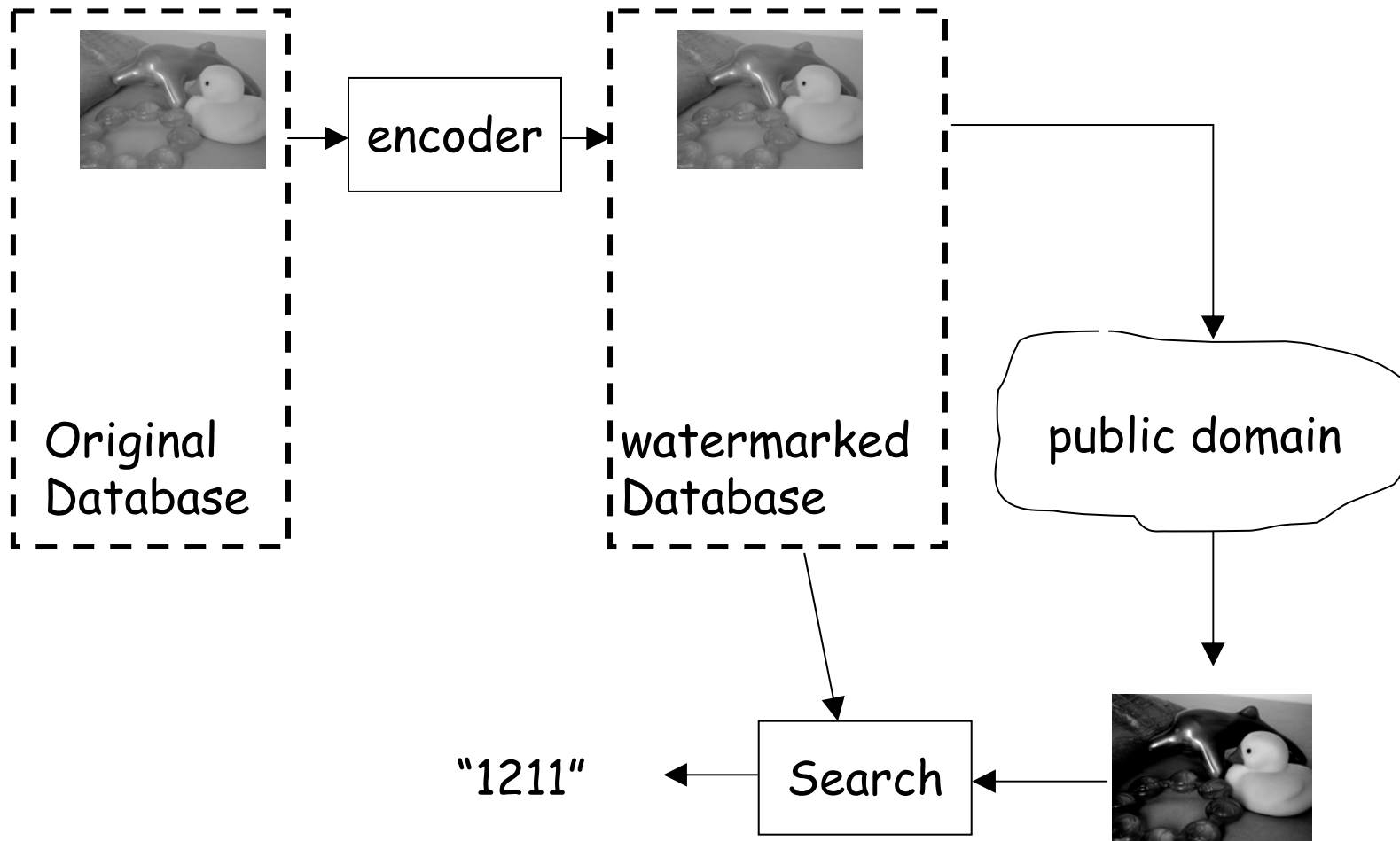


Index Tree

Buffer Zone



# Identification/tracking by Retrieval with WM.



## Problem Formulation:

Given  $\mathbf{I} = \langle I_1, \dots, I_n \rangle$ , a distortion constraint,  $e$ , and robustness  $\sigma^2$ , we want to preprocess  $\mathbf{I}$  to obtain the watermarked  $\mathbf{I}' = \langle I'_1, \dots, I'_n \rangle$  and an index tree.

1. The watermarked  $\mathbf{I}'$  satisfies the distortion constraint  $e$ ,

$$\sum_i \| I'_i - I_i \|^2 < e.$$

2. The index tree supports fast search, such that given the query  $I'_i$ , we can output  $i$  efficiently.

3. The searching is robust in the sense that if  $I'_i$  is corrupted by AWGN with power  $\sigma^2$ , the output is correct with high probability.

# Experiment

- A database of 2048 images.  
Each image is downsampled to  $64 \times 64$ .
- Robustness chosen to be 2  
(energy of image is normalized to 1)
- Average distortion: 0.00085  
Maximum distortion: 0.010

## Comparison

If only watermarking is used, with average distortion of 0.00085 and robustness 2, the theoretical maximum number of images allowed is

$$(1 + 0.00085/2)^{64 \times 64/2} < 3.$$

$$\text{capacity by watermarking} = (d/2) \log (1 + e/\sigma^2)$$

[1] M.Costa, Writing on dirty paper, *IEEE Trans. Info. Theory*, 29(3), 1983.

12 images (original) from the database.



Distortion

original Image



Distortion

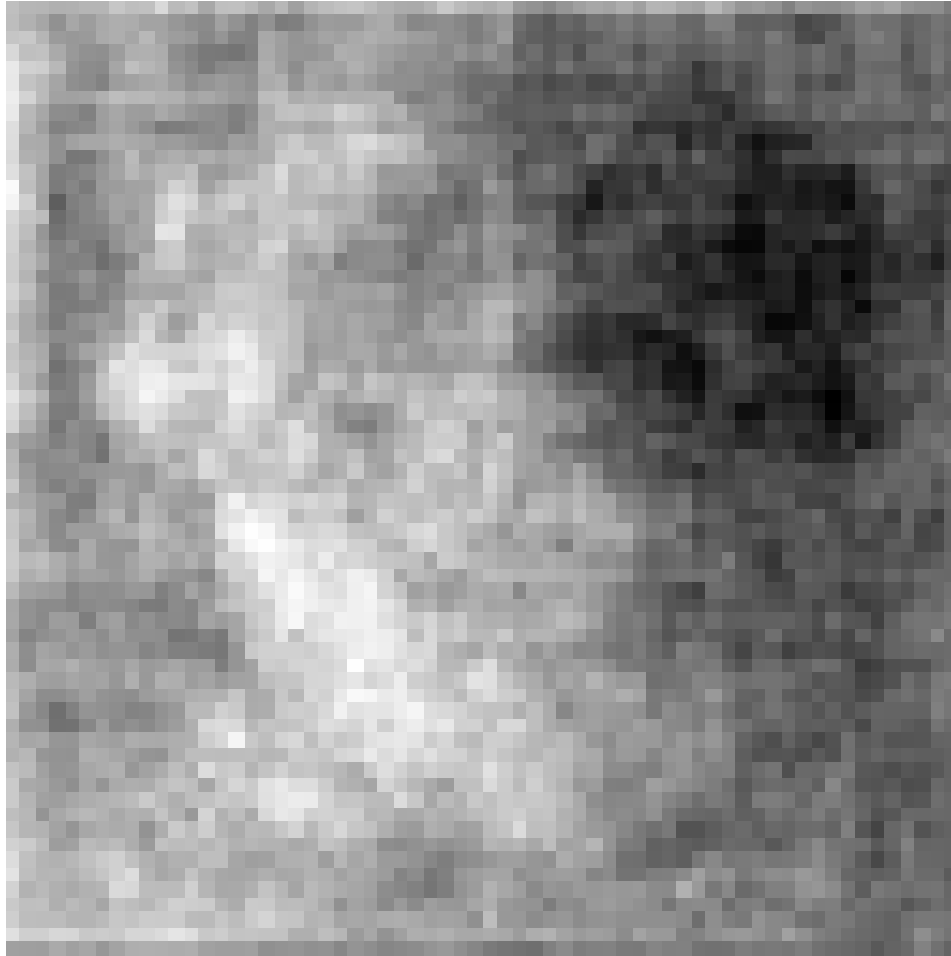
Watermarked Image





# Distortion

differences (original - watermarked)  
distortion: 0.010



# Distortion

original Image



Distortion

watermarked image



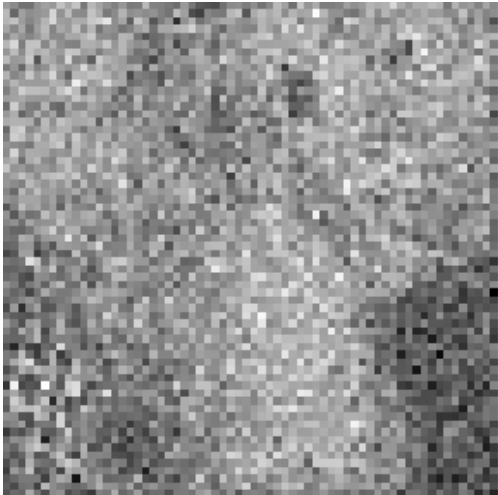
Distortion

Difference

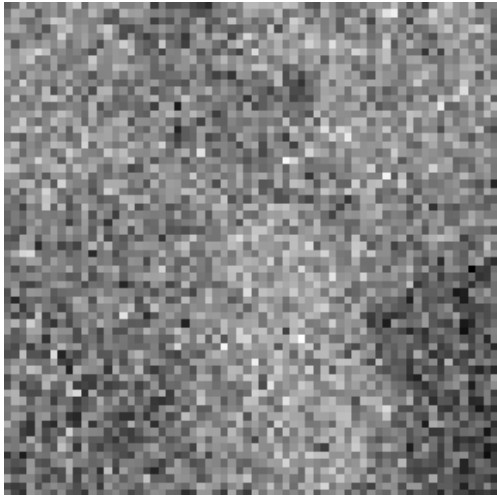
Distortion:0.0094



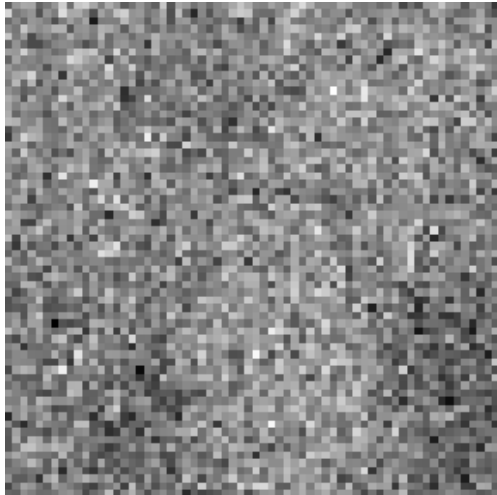
# Robustness



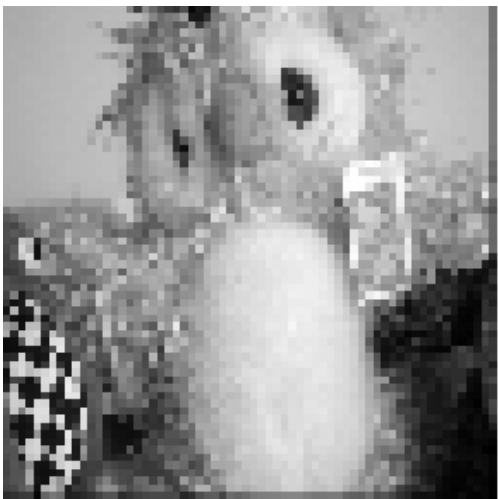
$\sigma^2 = 1$



$\sigma^2 = 2$

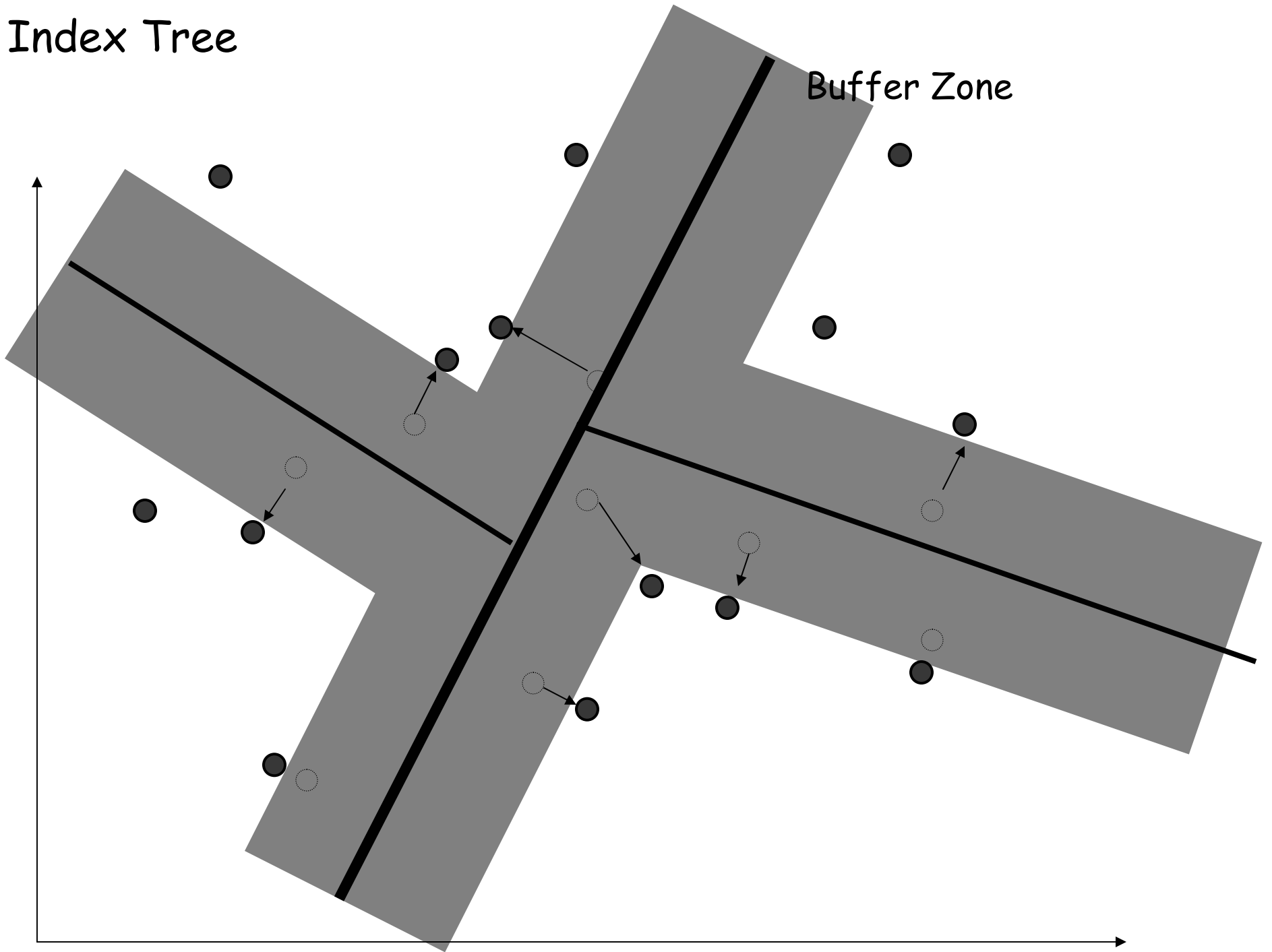


$\sigma^2 = 4$   
(655 in 1000)

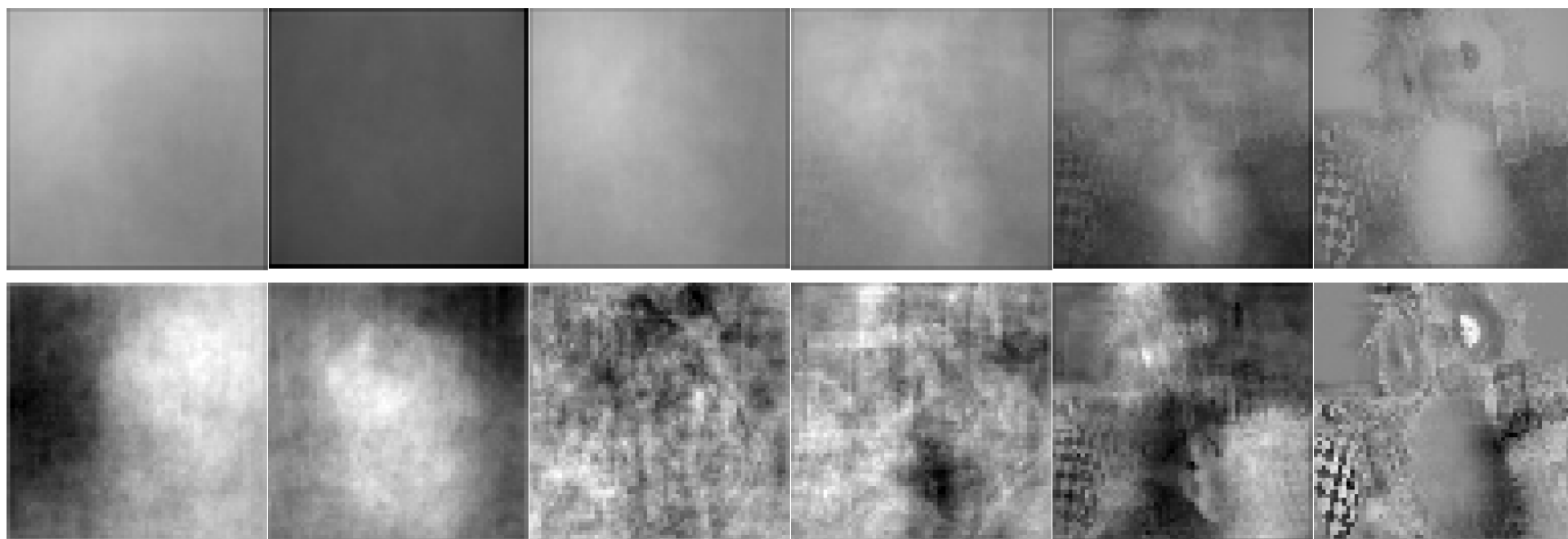


Index Tree

Buffer Zone

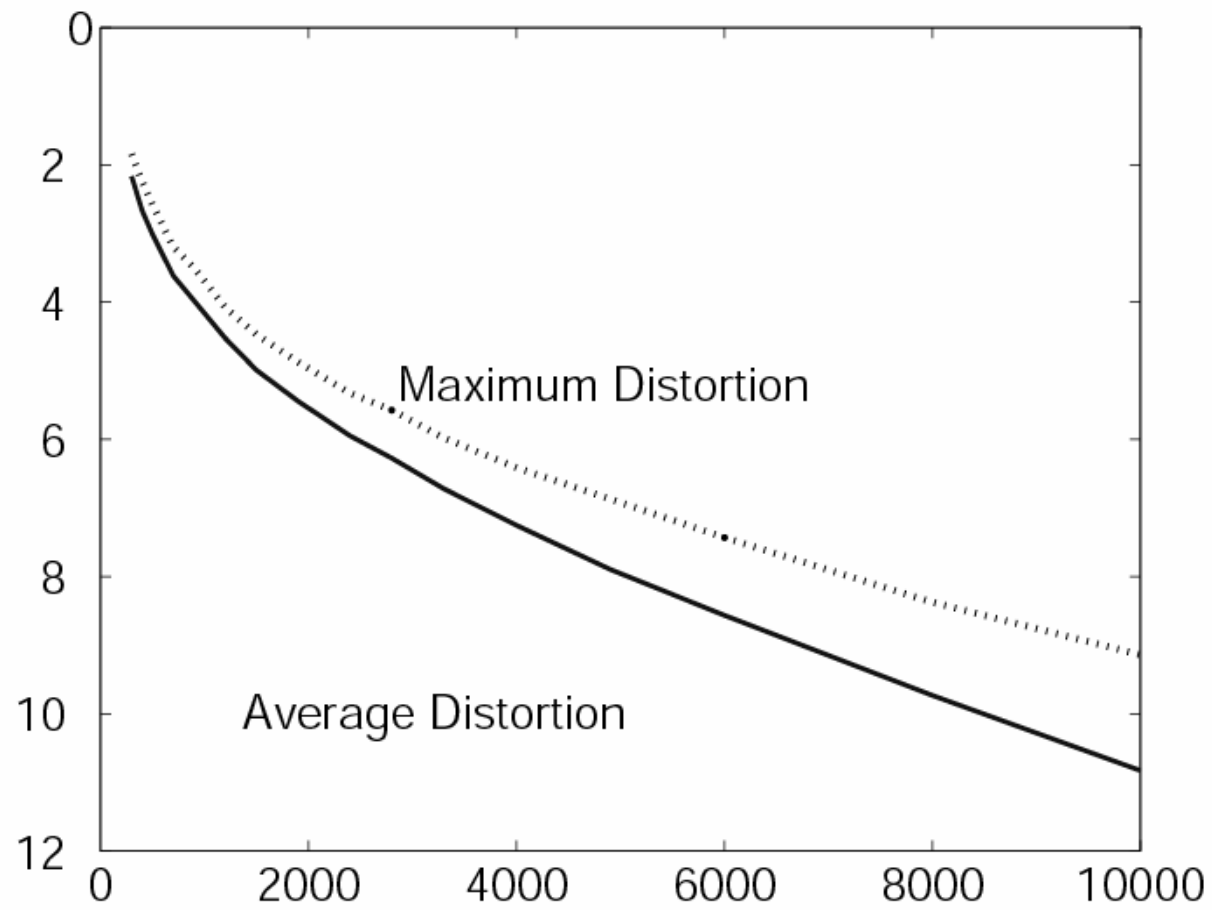


# Index Tree



1st level

8th level





# Variations and Future works

- Dynamic: allow the database to grow.
- Practical implementation: Consider geometric distortion (rotation, translation,...), compression, cropping, etc.
- Improving the clustering algorithm.
- Trade-off with the size of the index tree.

# Conclusion

- We introduce a variant of retrieval problem where the data-point can be distorted.
- Give an algorithm which is a combination of watermarking techniques and clustering algorithms.
- With small distortion, we can search fast.
- With knowledge of the database, and searching ability, we can improve watermarking performance.